

Notice:

- a) Term grading policy: Exam-3×40%.
- b) Total 125 points in this exam.
- c) Exam Time: 1:00PM–3:00PM, 11 Jan., 2023.

1. (25 pts) Evaluate the integral P.V.  $\int_{-\infty}^{\infty} \frac{\cos x + x \sin x}{x^2 + 1} dx$ .

2. (25 pts) Evaluate the integral P.V.  $\int_0^{\infty} \frac{dx}{\sqrt{x}(x^2 + 5x + 4)}$ .

3. (25 pts) Find the sum of the series  $\sum_{k=0}^{\infty} \frac{1}{16k^2 + 16k + 3}$  using the residue integration method.

4. (25 pts) Find the inverse Laplace transform of  $F(s) = \frac{s + 4}{s^2 + 6s + 11}$  using the residue integration method.

5. (25 pts) (a) Find the inverse Fourier transform of  $F(\omega) = \frac{1}{(1 - i\omega)^2}$  using the residue integration method.