

## Reference Solution

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DCChang

#1

**Solution (Maximum Power):** When no heat sink is used, the maximum device power dissipation is found from Equation (8.7) as

$$P_{D,\max} = \frac{T_{j,\max} - T_{\text{amb}}}{\theta_{\text{dev-case}} + \theta_{\text{case-amb}}} = \frac{150 - 30}{1.75 + 50} = 2.32 \text{ W}$$

When a heat sink is used, the maximum device power dissipation is found from Equation (8.6) as

$$\begin{aligned} P_{D,\max} &= \frac{T_{j,\max} - T_{\text{amb}}}{\theta_{\text{dev-case}} + \theta_{\text{case-snk}} + \theta_{\text{snk-amb}}} \\ &= \frac{150 - 30}{1.75 + 1 + 5} = 15.5 \text{ W} \end{aligned}$$

**Solution (Temperature):** The device temperature is  $T = 150^\circ\text{C}$  and the ambient temperature is  $T_{\text{amb}} = 30^\circ\text{C}$ . The heat flow is  $P_D = 15.5 \text{ W}$ . The heat sink temperature (see Figure 8.11) is found from

$$T_{\text{snk}} - T_{\text{amb}} = P_D \cdot \theta_{\text{snk-amb}}$$

or

$$T_{\text{snk}} = 30 + (15.5)(5) \Rightarrow T_{\text{snk}} = 107.5^\circ\text{C}$$

The case temperature is found from

$$T_{\text{case}} - T_{\text{amb}} = P_D \cdot (\theta_{\text{case-snk}} + \theta_{\text{snk-case}})$$

or

$$T_{\text{case}} = 30 + (15.5)(1 + 5) \Rightarrow T = 123^\circ\text{C}$$

#2

(a)

$$V_{DS} \geq V_{DS}(\text{sat}) = V_{GS} - V_{TN} = V_{GS}$$

$$V_{DS} = 10 - V_o(\text{max}) \text{ and } I_D = I_L = K_n (V_{GS})^2$$

$$\frac{V_o(\text{max})}{R_L} = K_n (V_{GS})^2$$

$$V_{GS} = \sqrt{\frac{V_o(\text{max})}{R_L \cdot K_n}}$$

$$\text{So } 10 - V_o(\text{max}) = \sqrt{\frac{V_o(\text{max})}{R_L \cdot K_n}} = \sqrt{\frac{V_o(\text{max})}{(5)(0.4)}}$$

$$[10 - V_o(\text{max})]^2 = \frac{V_o(\text{max})}{2}$$

$$100 - 20V_o(\text{max}) + V_o^2(\text{max}) = \frac{V_o(\text{max})}{2}$$

$$V_o^2(\text{max}) - 20.5V_o(\text{max}) + 100 = 0$$

$$V_o(\text{max}) = \frac{20.5 \pm \sqrt{(20.5)^2 - 4(100)}}{2} \Rightarrow \underline{V_o(\text{max}) = 8 \text{ V}}$$

$$i_L = \frac{8}{5} \Rightarrow \underline{i_L = 1.6 \text{ mA}}$$

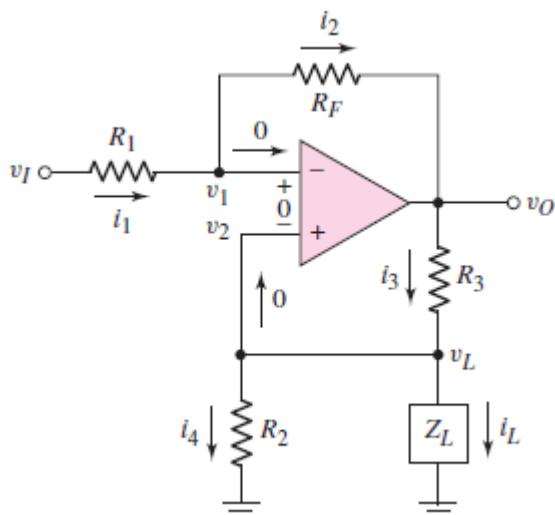
$$V_{GS} = \sqrt{\frac{i_L}{K_n}} = \sqrt{\frac{1.6}{0.4}} = 2 \text{ V} \Rightarrow \underline{V_I = 10 \text{ V}}$$

b.

$$\overline{P_L} = \frac{1}{2} \cdot \frac{(8)^2}{5} = 6.4 \text{ mW}$$

$$\overline{P_s} = \frac{20(1.6)}{\pi} = 10.2 \text{ mW}$$

$$\eta = \frac{\overline{P_L}}{\overline{P_s}} = \frac{6.4}{10.2} \Rightarrow \underline{\eta = 62.7\%}$$



$$\frac{v_I - i_L Z_L}{R_1} = \frac{i_L Z_L - v_O}{R_F}$$

$$\frac{v_O - i_L Z_L}{R_3} = i_L + \frac{i_L Z_L}{R_2}$$

$$\frac{R_F}{R_1} \cdot \frac{(i_L Z_L - v_I)}{R_3} = i_L + \frac{i_L Z_L}{R_2}$$

$$i_L \left( \frac{R_F Z_L}{R_1 R_3} - 1 - \frac{Z_L}{R_2} \right) = v_I \left( \frac{R_F}{R_1 R_3} \right)$$

In order to make  $i_L$  independent of  $Z_L$ , we can design the circuit such that the coefficient of  $Z_L$  is zero, or

$$\frac{R_F}{R_1 R_3} = \frac{1}{R_2}$$

$$i_L = -v_I \left( \frac{R_F}{R_1 R_3} \right) = \frac{-v_I}{R_2}$$

$$(a) \quad v_X = \left( \frac{v_I}{R} \right) (2R) + v_I = 3v_I$$

$$\frac{v_X - v_I}{2R} + \frac{v_X}{R} + \frac{v_X - v_O}{2R} = 0$$

$$v_X \left( \frac{1}{2R} + \frac{1}{R} + \frac{1}{2R} \right) - \frac{v_I}{2R} = \frac{v_O}{2R}$$

$$3v_I \left( \frac{2}{R} \right) - \frac{v_I}{2R} = \frac{v_O}{2R}$$

$$\text{so } \frac{v_O}{v_I} = 11$$

(b)

$$R = 30 \text{ k}\Omega, \quad v_I = -0.15 \text{ V}$$

$$\text{For } R_1: |i| = \frac{0.15}{30} \Rightarrow 5 \mu\text{A}$$

$$\text{For } R_2: |i| = 5 \mu\text{A}$$

$$v_X = 3v_I = -0.45 \text{ V}$$

$$\text{For } R_4: |i| = \frac{0.45}{30} \Rightarrow 15 \mu\text{A}$$

$$v_O = (11)(-0.15) = -1.65 \text{ V}$$

$$\text{For } R_3: |i| = \frac{1.65 - 0.45}{60} \Rightarrow 20 \mu\text{A}$$

$$(b) \frac{R_2}{R_1} = 2, \frac{R_4}{R_3} = 10, \frac{R_6}{R_5} = 11$$

$$V_0 = \left(1 + \frac{R_4}{R_3}\right) \left(\frac{R_6/R_5}{1 + R_6/R_5}\right) \cdot V_{02} - \frac{R_4}{R_3} V_{01}$$

$$= 11 \times \frac{11}{12} V_{02} - 10 V_{01}$$

$$= 10.083 V_{02} - 10 V_{01}$$

$$\begin{cases} V_{01} = 3V_{I1} - 2V_{I2} \\ V_{02} = 3V_{I2} - 2V_{I1} \end{cases}$$

$$\Rightarrow V_0 = 10.0833(3V_{I2} - 2V_{I1}) - 10(3V_{I1} - 2V_{I2})$$

$$= 50.25 V_{I2} - 50.167 V_{I1}$$

$$= A_{cm} \cdot \frac{V_{I1} + V_{I2}}{2} + A_d \cdot (V_{I2} - V_{I1})$$

$$= \left(A_d + \frac{A_{cm}}{2}\right) V_{I2} - \left(A_d - \frac{A_{cm}}{2}\right) V_{I1}$$

$$\Rightarrow \begin{cases} A_d + \frac{A_{cm}}{2} = 50.25 \\ A_d - \frac{A_{cm}}{2} = 50.167 \end{cases} \Rightarrow \begin{aligned} A_d &= 50.2085 \\ A_{cm} &= 0.083 \end{aligned}$$

$$\begin{aligned} CMRR(dB) &= 20 \log_{10} \left( \frac{50.2085}{0.083} \right) = 20 \log_{10}(604.92) \\ &= 55.634 (dB) \end{aligned}$$